

Wireless power transmission based on resonant electrical coupling

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COST IC1301 Workshop, Toulouse (September 30, 2014)
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Resonant magnetic coupling (2007): 4 coils (largest diameter of 60 cm, cross-sectional diameter of 6 mm), a 60 W light bulb, distance of 2 m, efficiency of 40%

Balanced trade-off between efficiency, range, simplicity, size and power transfer capability

$$\frac{V_0}{V_i} = \frac{-j\omega^2 M_{12} M_{23} M_{34} R_0}{M_{12}^2 M_{34}^2 \omega^4 + Z_1 Z_2 Z_3 Z_4 + \omega^2 (M_{12}^2 Z_3 Z_4 + M_{23}^2 Z_1 Z_4 + M_{34}^2 Z_1 Z_2)}$$
$$Z_1 = R_1 + j\omega L_1 - \frac{j}{\omega C_1}$$
$$Z_2 = R_2 + j\omega L_2 - \frac{j}{\omega C_2}$$
$$Z_3 = R_3 + j\omega L_3 - \frac{j}{\omega C_3}$$
$$Z_4 = R_4 + j\omega L_4 - \frac{j}{\omega C_4}$$
$$M_{12} = k_{12} \sqrt{L_1 L_2}$$
$$M_{23} = k_{23} \sqrt{L_2 L_3}$$
$$M_{34} = k_{34} \sqrt{L_3 L_4}$$

$$\frac{V_0}{V_i} = \frac{R_0 Z_3}{Z_1 Z_2 \left[Z_3 \left(j\omega (C_1 + C_2) + \frac{1}{Z_1} + \frac{1}{Z_2} \right) - \omega^2 C_1 C_2 + j\omega \left(\frac{C_1 C_2}{Z_2 Z_1} + \frac{1}{Z_1 Z_2} \right) \right]}$$
$$Z_1 = R_1 + j\omega L_1$$
$$Z_2 = R_2 + j\omega L_2$$
$$Z_3 = j\omega \frac{C_1 C_2}{C_3 + C_4}$$

Available power gain: $\frac{P_0}{P_A} = \frac{4R_0}{R_0} \left| \frac{V_0}{V_i} \right|^2$

Parameter	Value
R_1, R_0	50 Ω
R_1, R_4	2 Ω
R_2, R_3	10 Ω
L_1, L_4	1 μ H
L_2, L_3	28 μ H
C_1, C_4	140 pF
C_2, C_3	5 pF
k_{12}, k_{34}	0.1

$C_4 = C_3$

k_{23}	0.001	0.002	0.005	0.008	0.015
C_3 (pF)	0.02	0.04	0.06	0.1	0.18

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distance (cm)	10	20	60	90	500
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angle (°)	0	40	90	180	270
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Conclusions:

Systems based on resonant magnetic coupling are currently very popular in the literature, systems based on resonant electrical coupling are not; The duality between resonant magnetic coupling and resonant electrical coupling is quite noticeable; It was not yet possible to obtain a complete match between experimental results and theory, but some key aspects were confirmed.